

**NAME**

PHASE2 – Pivot a canonical-form linear programming tableau to optimality.

**SYNOPSIS**

**CALL PHASE2(T,LDT,BASIS,MP,N,ROWS,MR, RC)**

T(LDT,\*) is the REAL\*8 input LP tableau  
 LDT is the INTEGER\*4 leading dimension of T  
 BASIS(N) is the INTEGER\*4 input/output vector of basic column row indices, 0 for nonbasic  
 MP is the INTEGER\*4 total number of rows in the LP including the objective  
 N is the INTEGER\*4 number of variables in the LP  
 ROWS(MR) is the INTEGER\*4 input vector of the row indices in the problem  
 MR is the INTEGER\*4 input number of rows in use including the objective  
 RC is the INTEGER\*4 return code; 0 => optimal; >0 => unbounded in column RC

**DESCRIPTION**

First the routine finds the most negative cost entry in T. Then it uses MINR to find the minimum-ratio row in that column, or returns with RC set to that column index if no element in the column is greater than 1.D-06. Finally it pivots on the minimum-ratio element, updating T and BASIS. This process is repeated until no negative cost entries remain, when it returns with RC=0.

**DIAGNOSTICS**

On output these are the possible RC values:

0 all went well  
 J the index of a column in which the linear program is unbounded

**LINKAGE**

gfortran source.f -L\${HOME}/lib -lmisc

**AUTHOR**

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**REFERENCE**

[1] Kupferschmid, Michael, "Introduction to Mathematical Programming"

**EXAMPLE**

```

PARAMETER (LDT=4,MP=4,N=7,MR=4)
INTEGER*4 ROWS (MR) /1,2,3,4/,BASIS (7),RC
REAL*8 T (LDT,1+N)/0.0D0, 1.6D2, 5.0D1, 6.0D1,
;          -9.0D1, 7.0D0, 1.0D0, 2.0D0,
;          -1.5D2, 1.0D1, 3.0D0, 4.0D0,
;          -6.0D1, 8.0D0, 1.0D0, 1.0D0,
;          -7.0D1, 1.2D1, 1.0D0, 3.0D0,
;          0.0D0, 1.0D0, 0.0D0, 0.0D0,
;          0.0D0, 0.0D0, 1.0D0, 0.0D0,
;          0.0D0, 0.0D0, 0.0D0, 1.0D0/
DO 1 I=1,MP
    WRITE (6,901) (T (I,J),J=1,1+N)
901    FORMAT (8 (1X,F7.1))
1 CONTINUE
CALL PHASE2 (T,LDT,BASIS,MP,N,ROWS,MR,RC)
WRITE (6,900)
900 FORMAT (' ')
DO 2 I=1,MP
    WRITE (6,901) (T (I,J),J=1,1+N)
2 CONTINUE
STOP
END

```

This example (which is from [1] page 72) produced the following output:

```

unix[1] a.out
  0.0   -90.0  -150.0   -60.0   -70.0    0.0    0.0    0.0
160.0    7.0   10.0    8.0   12.0    1.0    0.0    0.0
 50.0    1.0    3.0    1.0    1.0    0.0    1.0    0.0
 60.0    2.0    4.0    1.0    3.0    0.0    0.0    1.0

2325.0   0.0    0.0   18.8   76.3    7.5    0.0   18.8
  5.0    1.0    0.0    2.8    2.3    0.5    0.0   -1.3
  7.5    0.0    0.0    1.6   -0.1    0.3    1.0   -1.4
 12.5    0.0    1.0   -1.1   -0.4   -0.3    0.0    0.9
unix[2]

```